

ERRATA

Mathematics for Australia 10A

Worked Solutions

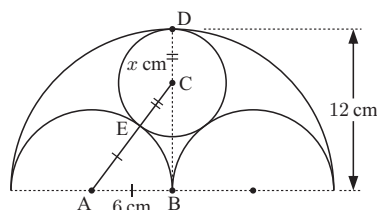
2013 First Edition

page 19 **CHAPTER 1 PRACTICE TEST 1C**, Question **1 a ii** should read:

- 1 a i** 1 hour = 60 minutes
 $= 60 \times 60$ seconds
 $\{1 \text{ minute} = 60 \text{ s}\}$
 $= 3600$ seconds
 and $2.998 \times 10^8 \times 3600$
 $= 1.07928 \times 10^{12}$
 $\approx 1.079 \times 10^{12}$
 So, light travels about 1.079×10^{12} m in one hour (in a vacuum).
- ii** 1 day = 24 hours
 $= 24 \times 3600$ seconds $\{\text{using a i}\}$
 $= 86400$ seconds
 and $2.998 \times 10^8 \times 86400$
 $= 2.590272 \times 10^{13}$
 $\approx 2.590 \times 10^{13}$
 So, light travels about 2.590×10^{13} m in one day (in a vacuum).

page 145 **CHAPTER 6 EXERCISE 6E**, Question **14 a ii** should read:

- 14 a ii** Consider the 'upper' semi-circle:



Suppose the radius of the smallest circle is x cm and $CB = DB - DC = (12 - x)$ cm. We construct $[AC]$, which passes through E .

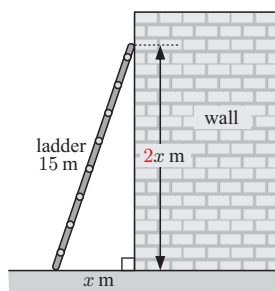
- Now, $AE = 6$ cm $\{\text{from a i}\}$
 $\therefore AC = (6 + x)$ cm
 $\therefore (6 + x)^2 = 6^2 + (12 - x)^2$ $\{\text{Pythagoras in } \triangle ABC\}$
 $\therefore 36 + 12x + x^2 = 36 + 144 - 24x + x^2$
 $\therefore 12x = 144 - 24x$
 $\therefore 36x = 144$
 $\therefore x = 4$
 \therefore the radius of the smallest circles is 4 cm.

page 147 **CHAPTER 6 EXERCISE 6F**, Questions **10** and **11** should begin with measures in metres:

- 10** Let the diagonal $[BD]$ be $2x$ m.
11 Consider the pyramid on top of the tower. Let the diagonal $[AC]$ be $2x$ m.

page 153 **CHAPTER 6 PRACTICE TEST 6B**, Question **7** should have correctly labelled diagram:

- 7** Suppose the foot of the ladder is x m from the wall.
 \therefore the ladder reaches $2x$ m up the wall.
 $\therefore x^2 + (2x)^2 = 15^2$ $\{\text{Pythagoras}\}$
 $\therefore x^2 + 4x^2 = 225$
 $\therefore 5x^2 = 225$
 $\therefore x^2 = 45$
 $\therefore x = \sqrt{45}$ $\{\text{as } x > 0\}$
 $\therefore 2x = 2\sqrt{45}$
 $\therefore 2x \approx 13.42$ m



The ladder reaches about 13.4 m up the wall.

1 a $C = 2\pi r$ where $r = 4.2$
 $\therefore C = 2 \times \pi \times 4.2$
 ≈ 26.4
 \therefore the circumference is approximately 26.4 cm.

b $C = 2\pi r$ where $C = 112$
 $\therefore 112 = 2\pi r$
 $\therefore r = \frac{112}{2\pi}$
 ≈ 17.8
 \therefore the radius is approximately 17.8 cm.

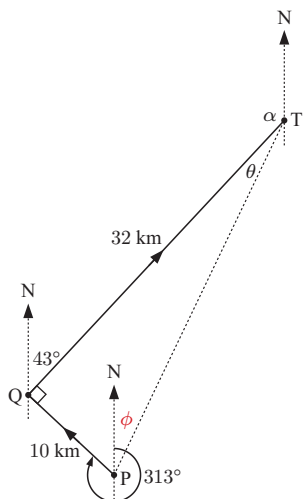
2 g $x^2 + 1 = 3x$
 $\therefore x^2 - 3x + 1 = 0$ which has
 $a = 1, b = -3, c = 1$
 $\therefore x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(1)(1)}}{2(1)}$
 $\therefore x = \frac{3 \pm \sqrt{9 - 4}}{2}$
 $\therefore x = \frac{3 \pm \sqrt{5}}{2}$

h $2x^2 = 2x - 3$
 $\therefore 2x^2 - 2x + 3 = 0$ which has
 $a = 2, b = -2, c = 3$
 $\therefore x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(2)(3)}}{2(2)}$
 $\therefore x = \frac{2 \pm \sqrt{4 - 24}}{4}$
 $\therefore x = \frac{2 \pm \sqrt{-20}}{4}$
 but $-20 < 0$
 \therefore no real solutions exist.

2 d $AB = \sqrt{(-\sqrt{2} - \sqrt{2})^2 + (0 - 0)^2}$
 $= \sqrt{(-2\sqrt{2})^2 + 0^2}$
 $= \sqrt{8}$ units
 $AC = \sqrt{(0 - \sqrt{2})^2 + (-\sqrt{5} - 0)^2}$
 $= \sqrt{(-\sqrt{2})^2 + (-\sqrt{5})^2}$
 $= \sqrt{2 + 5}$
 $= \sqrt{7}$ units
 $BC = \sqrt{(0 - -\sqrt{2})^2 + (-\sqrt{5} - 0)^2}$
 $= \sqrt{(\sqrt{2})^2 + (-\sqrt{5})^2}$
 $= \sqrt{2 + 5}$
 $= \sqrt{7}$ units
 Since $AC = BC$, triangle ABC is isosceles.

e $AB = \sqrt{(-\sqrt{3} - \sqrt{3})^2 + (1 - 1)^2}$
 $= \sqrt{(-2\sqrt{3})^2 + 0^2}$
 $= \sqrt{12}$ units
 $AC = \sqrt{(0 - \sqrt{3})^2 + (-2 - 1)^2}$
 $= \sqrt{(-\sqrt{3})^2 + (-3)^2}$
 $= \sqrt{3 + 9}$
 $= \sqrt{12}$ units
 $BC = \sqrt{(0 - -\sqrt{3})^2 + (-2 - 1)^2}$
 $= \sqrt{(\sqrt{3})^2 + (-3)^2}$
 $= \sqrt{3 + 9}$
 $= \sqrt{12}$ units
 Since $AB = AC = BC$, triangle ABC is equilateral.

12



$\widehat{NPQ} = 360^\circ - 313^\circ = 47^\circ$ {angles at a point}

$\widehat{TQP} = 180^\circ - 43^\circ - 47^\circ$ {cointerior angles}
 $= 90^\circ$

a $TP^2 = 10^2 + 32^2$ {Pythagoras}

$\therefore TP = \sqrt{10^2 + 32^2}$ {as $TP > 0$ }

$\therefore TP \approx 33.5$

$\tan \theta = \frac{10}{32}$ { $\tan \theta = \frac{OPP}{ADJ}$ }

$\therefore \theta = \tan^{-1}\left(\frac{10}{32}\right)$

$\therefore \theta \approx 17.4^\circ$

$\alpha = 180^\circ - 43^\circ = 137^\circ$ {cointerior angles}

$\phi = 180^\circ - \alpha - \theta$ {cointerior angles}

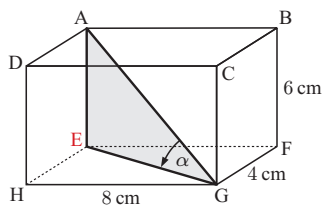
$\approx 180^\circ - 137^\circ - 17.4^\circ$

$\approx 25.6^\circ$

So, the trawler is about 33.5 km from P, on a bearing of $\approx 025.6^\circ$.

b The trawler must sail on a bearing of $360^\circ - 137^\circ - 17.4^\circ \approx 206^\circ$.

10 b



$$(EG)^2 = 4^2 + 8^2 \quad \{\text{Pythagoras}\}$$

$$\therefore EG = \sqrt{80}$$

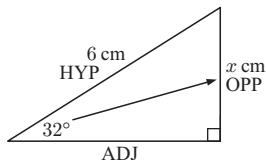
$$\tan \alpha = \frac{6}{\sqrt{80}} \quad \left\{ \tan \alpha = \frac{\text{OPP}}{\text{ADJ}} \right\}$$

$$\therefore \alpha = \tan^{-1}\left(\frac{6}{\sqrt{80}}\right)$$

$$\therefore \alpha \approx 33.9^\circ$$

$$\therefore \widehat{AGE} \approx 33.9^\circ$$

3 a



$$\sin 32^\circ = \frac{x}{6} \quad \left\{ \sin \theta = \frac{\text{OPP}}{\text{HYP}} \right\}$$

$$\therefore 6 \times \sin 32^\circ = x \quad \{\text{multiplying both sides by 6}\}$$

$$\therefore x \approx 3.18 \quad \{\text{calculator}\}$$

4 a

Distance d (m)	Frequency	Interval midpoint	Product
$20 \leq d < 30$	2	25	50
$30 \leq d < 40$	6	35	210
$40 \leq d < 50$	26	45	1170
$50 \leq d < 60$	12	55	660
$60 \leq d < 70$	3	65	195
$70 \leq d < 80$	1	75	75
Total	50		2360

\therefore mean

$$= \frac{\text{sum of data values}}{\text{the number of data values}}$$

$$\approx \frac{2360}{50}$$

$$\approx 47.2 \text{ m}$$

2 a $\frac{BC}{\sin 60^\circ} = \frac{12}{\sin 40^\circ}$ {sine rule}

$$\therefore BC = \frac{12 \times \sin 60^\circ}{\sin 40^\circ}$$

$$\therefore BC \approx 16.168 \text{ m}$$

$$\therefore BC \approx 16.2 \text{ m}$$

$$DC = BC - BD$$

$$\approx 16.2 - 6$$

$$\therefore DC \approx 10.2 \text{ m}$$

b Area = $\frac{1}{2}ab \sin C$

$$\therefore 13.5 = \frac{1}{2} \times 6 \times BE \times \sin 40^\circ$$

$$\therefore BE = \frac{9}{2 \times \sin 40^\circ}$$

$$\therefore BE \approx 7.00 \text{ m}$$

10 c $0.442 > 0.438 > 0.120$

\therefore Carina is now most likely to win at 44.2%, followed by Pia at 43.8%, and now Larry is least likely to win at only 12.0%.

4 a The graph of $y = g(x)$ is obtained by translating $f(x) = -\frac{1}{2}x - 1$ 4 units upwards.

$$\therefore g(x) = f(x) + 4$$

$$= -\frac{1}{2}x - 1 + 4$$

$$= -\frac{1}{2}x + 3$$

b The graph of $y = g(x)$ is obtained by translating $f(x) = \frac{3}{2}x + 1$ 2 units to the right.

$$\therefore g(x) = \frac{3}{2}(x - 2) + 1$$

$$= \frac{3}{2}x - 3 + 1$$

$$= \frac{3}{2}x - 2$$

7 a iii $\log 250 \approx 2.397\ 940\ 009$
 ≈ 2.398

iv $\log\left(\frac{1}{250}\right) \approx -2.397\ 940\ 009$
 ≈ -2.398

4 c When $N = 200$, $200 = 10 \times 1.3^t$

$$\therefore 1.3^t = 20$$

$$\therefore \log(1.3^t) = \log 20 \quad \{\text{taking the log of both sides}\}$$

$$\therefore t \log 1.3 = \log 20 \quad \{\log(a^n) = n \log a\}$$

$$\therefore t = \frac{\log 20}{\log 1.3}$$

$$\therefore t \approx 11.4$$

It will take about 11.4 weeks for Danielle's blog to have 200 followers.