### MATHEMATICS FOR THE INTERNATIONAL STUDENT MATHEMATICS HL (as at 23 April 2008)

# ERRATA FOR INITIAL PRINT RUN

### TEXT

page 153 Exercise 7L

3 v(t) should be:  $-\frac{1}{2}t^2 + \frac{1}{2}t + 15$ 

### page 154 Exercise 7L

- 3 new parts **b**, **c** and **d**:
  - **b** After how many seconds did the car reach its maximum velocity? Explain why this may have happened.
  - c What was the maximum velocity reached?
  - **d** How long does it take for the car to stop?

### page 209 E - Combinations

Highlighted box should read:  $C_r^n = \frac{n(n-1)(n-2)\dots(n-r+3)(n-r+2)(n-r+1)}{r(r-1)(r-2)\dots 3} = \frac{n!}{2}$ 

### page 446 Example19

**b** missing = sign in calculation of **n**:

$$\mathbf{n} = \dots = \begin{bmatrix} -1\\ -10\\ -6 \end{bmatrix} = - \begin{bmatrix} 1\\ 10\\ 6 \end{bmatrix}$$

# page 516 Exercise 19H

4 calculator instructions for **b** should use binomcdf, i.e., in **b**  $P(X \le 3) = \text{binomcdf}(5, 0.9, 3)$ 

### ANSWERS

### page 780 Exercise 7L

3 new answers corresponding to new question:

- **a** 15 m/s
- **b**  $\frac{1}{2}$  sec.; since the car was travelling downhill, it was accelerating.  $\therefore$  when the break was applied, the speed of the vehicle still increased for a short time.
- c  $15\frac{1}{8}$  m/s d 6 seconds

### page 796 Exercise 14N

**3 b i** 
$$\mathbf{P}^n = \begin{bmatrix} n+1 & n \\ -n & 1-n \end{bmatrix}$$
 for all  $n \in Z^+$ 

# ERRATA FOR FIRST REPRINT

# TEXT

4

page 276 Exercise 13C

Question should finish: ...time difference between high tides is about 12.4 hours.

### page 302 Exercise 13N

8 f  $\frac{(1-\cot\theta)^2}{\csc^2\theta} + \sin 2\theta = 1$ 

page 303 Exercise 130

5 RHS of equation should be:  $\frac{1-\cos 2n\theta}{2\sin \theta}$ 

### page 384 Exercise 15J.1

1 There is a diagram missing next to the blue highlighted box.



page 642 Exercise 24C.1 4 question should read: ...to show that  $\arctan(5) - \arctan(\frac{2}{3}) = \frac{\pi}{4}$ 

page 644 Exercise 24D

3 radius of lake should be 2 km, not 4 km.

### page 649 Exercise 24E

16 the wheel rotates in a clockwise direction

page 726 Review Set 29A

3 ... deduce that  $y = \sqrt{2x+4} - 2$ 

### page 732 Example 4

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The diagram is missing some labels: A P(X=x)
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page 738 **Property of Var(X)** Highlighted text should be:  $Var(x) = E(X^2) - \{E(X)\}^2$  i.e.,  $Var(X) = E(X^2) - \mu^2$ 

page 740 Exercise 30E.2

1 Question should finish: ...standard deviation of the Y distribution.

### ANSWERS

*page 764* **Review Set 1A 2 b iv** no

*page 765* Exercise 2D 14 £53 519.29

page 766 **Review Set 2A** 9  $u_n = \frac{1}{6} \times 2^{n-1}$  or  $-\frac{1}{6} \times 2^{n-1}$ 

page 767 Exercise 3G 5 d label on graph should be:  $y = 3 - 2^{-x}$ 

page 767 Exercise 3H

- **4 a** 12 bears
- **b** 146 bears
- page 767 Exercise 3I 4 yes

page 768 Exercise 4A 6 d  $-\frac{1}{2}$ 

page 769 Exercise 4E

2 b 221 min 5 15.8°C

page 769 Exercise 4F 1 6.17 years, i.e., 6 years 62 days

*page* 770 Exercise 5A **13 a i** 64.6 amps

page 770 Exercise 5C

 $\begin{array}{ccc} \mathbf{4} \mathbf{c} & \sqrt{x} \\ \mathbf{f} & \frac{1}{\sqrt[3]{g}} \end{array}$ 

page 775 Exercise 6E

**2 b** Vertically stretch, factor  $\frac{1}{6}$  then translate by  $\begin{vmatrix} -1 \\ -2 \end{vmatrix}$ .

*page 777* Exercise 7B.24 b i vertex of (2, -4) should be marked on graph

page 780 Exercise 7H

- **6 g iv** graph x-intercepts are: -4 and -2
- i iv graph x-intercepts are:  $4 2\sqrt{5}$  and  $4 + 2\sqrt{5}$

difference between his

page 780 Exercise 7I.1

2 a, b, d, f

### page 783 Exercise 8G.1

**3 c** should be: For  $x \in \left]-\infty, 0\right[$  or  $\left]0.627, \infty\right[$ 

page 786 Exercise 11D.1

**3 b** AP =  $\frac{\pi}{3}$ 

page 788 Exercise 13B.1



page 788 Exercise 13C 1 a  $T \doteq 6.5 \sin \frac{\pi}{6}(t - 4.5) + 20.4$ 

**2 a**  $T \doteq 4.5 \sin \frac{\pi}{6} (t - 4.5) + 20.4$  **3 a**  $T \doteq 4.5 \sin \frac{\pi}{6} (t - 4.5) + 11.5$ **4 a**  $H \doteq 7 \sin 0.507 (t - 6.2)$ 

page 791 Exercise 13K.2

1j 1

page 791 Exercise 13O 1 b  $\frac{1}{1-\sin x}$  as  $-1 \le \sin x \le 1$ 2 c  $\frac{\sin 2nx}{2\sin x}$ 

page 792 Review Set 13A

5  $T \Rightarrow 7.05 \sin \frac{\pi}{6}(t-4.5) + 24.75$ 10 c 0.5 < t < 2.5 and 6.5 < t < 8

page 792 Exercise 14B



page 794 Exercise 14L 4 c x = 2, y = 4, z = -1

page 798 Exercise 15E.1

**2** a 
$$\overrightarrow{AB} = \begin{bmatrix} 4\\ -1\\ -3 \end{bmatrix}, \overrightarrow{BA} = \begin{bmatrix} -4\\ 1\\ 3 \end{bmatrix}$$

page 798 Exercise 15G

4 b parallelogramc not parallelogram

page 800 Review Set 15B

1 c  $\sqrt{61}$  units

page 802 Exercise 17A.1

page 804 Exercise 17F

**1 b i**  $a_1 = ka_2, b_1 = kb_2, c_1 = kc_2$  for some k **ii**  $a_1 = ka_2, b_1 = kb_2, c_1 = kc_2, d_1 = kd_2$  for some k

page 804 Review Set 17A

**7 a** X23,  $x_1 = 2 + t$ ,  $y_1 = 4 - 3t$ ,  $t \ge 0$ 

- **b** Y18,  $x_2 = 9 t$ ,  $y_2 = 3 + 2a + at$ ,  $t \ge 0$
- **c** interception occurred at 2:20:30 pm
- **d**  $\theta = 192^{\circ}, \doteq 4.82 \text{ km/min}$

page 805 Exercise 18B.1

**4 a** mean: 3.19, median: 0, mode: 0

page 806 Exercise 18C

4 b 36 c i 0.527 ii 0.030

*page 806* Exercise 18D.1 5 a iv 7

*page 807* Exercise 18F 1 a 4.97

*page 809* Exercise 19I 11 b P(A or B) = P(A) + P(B) - P(A and B)

page 810 Exercise 19L

1  $\Rightarrow 0.655$ 5 a  $\frac{2}{5}$ 

*page 810* Exercise 20A.1 1 a 96.2 km/h

*page 811* Exercise 21D 1 n 8*x* - 4

**3 c** 2x - 10

*page 812* Exercise 22A 3 f 5.777

*page 812* Exercise 22C.1

3 units should be  $cm/s^2$ , not  $m/s^2$ 

page 815 Exercise 22F

**2 f i** local min. at (1, 0)

- ii no points of inflection
- iii increasing for  $x \ge 1$ , decreasing for  $x \le 1$



page 816 Exercise 22G14 between A and N, 2.578 m from N

page 817 Review Set 22A base is 1.26 m square, height 0.630 m 5 a page 818 Exercise 23D 13 c as  $t \to \infty$ ,  $v(t) \to 100$  cm/s (below) page 818 Review Set 23A 1 c  $3x^2 + y^4 + 4xy^3 \frac{dy}{dx} = e^y + xe^y \frac{dy}{dx}$ page 819 Exercise 24A  $2x\cos(x^2)$ 3 a  $-\frac{1}{2\sqrt{x}}\sin(\sqrt{x})$ b  $-\frac{\sin x}{2\sqrt{\cos x}}$ с d  $2\sin x\cos x$  $-3\sin x\cos^2 x$ e  $-\sin x \sin(2x) + 2\cos x \cos(2x)$ f  $\sin x \sin(\cos x)$ g  $-12\sin(4x)\cos^2(4x)$ h  $-\frac{\cos x}{\sin^2 x}$ i  $\frac{2\sin(2x)}{\cos^2(2\pi)}$ i k l 7 a rising rising at 2.731 m per hour b page 819 Review Set 24B  $\frac{-\sqrt{x}\csc^2 x - \frac{1}{2}x^{-\frac{1}{2}}\cot x}{2x\sqrt{x}\sin^2 x} \equiv -\frac{\cos x \sin x + 2x}{2x\sqrt{x}\sin^2 x}$ 2 i

page 820 Exercise 24E  
16 b 
$$100\pi$$
 radians per second

page 820 Review Set 24A increasing for  $\frac{3\pi}{2} < x < 2\pi$ , decreasing for  $0 < x < \frac{\pi}{2}$ 5 b

### page 822 Exercise 26B $45\frac{3}{4}$ units<sup>2</sup> 2 b

page 824 Exercise 28A.1  $\frac{1024\pi}{5}$  units<sup>3</sup> 6 b

### page 824 Exercise 28B



 $\doteq 237 \text{ units}^3$ с

page 825 Exercise 29D.3  $4 \quad y = Axe^{2x^2}$ 

page 825 Review Set 29B

**2 b**  $\sqrt{x^2 - 4} + 2 \arccos(\frac{2}{\pi}) + c$ 

page 825 Exercise 30A **2 a ii**  $0 \leq x \leq 200 \text{ mm}$ 

page 826 Exercise 30B  $6 \quad (6,1) \quad (6,2) \quad (6,3) \quad (6,4) \quad (6,5) \quad (6,6)$ 5 a 5(5, 1) (5, 2) (5, 3) (5, 4) (5, 5) (5, 6)(4, 1) (4, 2) (4, 3) (4, 4) (4, 5) (4, 6)roll 1 4 (3, 1) (3, 2) (3, 3) (3, 4) (3, 5) (3, 6)3 (2, 1) (2, 2) (2, 3) (2, 4) (2, 5) (2, 6) $\mathbf{2}$ 1 (1, 1) (1, 2) (1, 3) (1, 4) (1, 5) (1, 6)2 3 4 roll 2 page 827 Exercise 30F **4 b** ≑ 0.00246 page 827 Exercise 30H **4 b** = ⇒ 0.392 page 827 Exercise 30J.1 3 c 2.15%, 95.4% page 828 Exercise 30K.1 **3 b** 0.524 page 828 Exercise 30K.3 **2 c**  $k \doteq -1.089$ ERRATA FOR SECOND REPRINT TEXT page 37 Opening Problem The opening paragraph should read: "A circular stadium consists of sections as illustrated, with aisles in between. The diagram shows the tiers of concrete for the final section, Section K. Seats are to be placed along every concrete step, with each seat being 0.45 m wide. AB, the arc at the front of the first row is 14.4 m long, while CD, the arc at the back of the back row is 20.25 m long.' The angle  $32^{\circ}$  in the diagram should be removed. page 53 Exercise 2G 8

last paragraph should be: "At the end of the first quarter the amount owed,  $A_1$ , is given by  $8000 \times 1.03 - R$ , where R is the amount of each repayment."

### ERRATA FOR THIRD REPRINT TEXT

*page 392* Length of  $\mathbf{a} \times \mathbf{b}$  proof

The top line of the page should read:

 $=(a_1^2 + a_2^2 + a_3^2)(b_1^2 + b_2^2 + b_3^2) - (a_1b_1 + a_2b_2 + a_3b_3)^2$ 

page 392 Exercise 15K.2

5 c question should finish: ... prove that  $\mathbf{a} + \mathbf{b} = k\mathbf{c}$  for some scalar k.

### page 436 Exercise 17B.3

3 a question should be: Find in terms of **i** and **j** and velocity vector of the liner.

page 447 Example 21



### page 578 Exercise 22B

- 6 b If the birth rate is 6%, the maximum carrying capacity is 24000 and 5% is harvested, find the stable population.
  - **c** If the harvest changes to 4%, what will the stable population increase to?

### page 699 Definite integrals

Integral in Fundamental Theorem of Calculus definition should be:

$$\int_{a}^{b} f(x) \, dx = F(b) - F(a)$$

### page 709 Exercise 28B

5 diagram should be:



### ANSWERS

*page* 776 **Review set 6A** 4 c ii 0.9

page 788 Exercise 13B.1



page 803 Exercise 17B.4

1 a Points B and C should be swapped in the diagram.

### ERRATA FOR FOURTH REPRINT

## TEXT

- page 433 Exercise 17B.2
- **2 b** question should finish:
  - ... velocity reaches (18, 21) in 10 seconds

4 d question should start: If they start at 6:00 am, find the time...

### ANSWERS

page 803 Exercise 17B.2 2 b  $\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -2 \\ 6 \end{bmatrix} + \frac{t}{2.5} \begin{bmatrix} 20 \\ 15 \end{bmatrix}, t \in \mathbb{R}$ 

**4 d** 10:12 am

# ERRATA FOR FIFTH REPRINT

# TEXT

page 94 Review set 4A 2 c  $\log (10^a \times 10^{b+1})$ 

page 701 Exercise 27D

2 The region is defined for  $x \ge 0$ .

# ANSWERS

page 788 Exercise 13C

- 1 **a**  $T \doteq 6.5 \sin \frac{\pi}{6} (t 4.5) + 20.5$
- **2 a**  $T \doteq 4.5 \sin \frac{\pi}{6} (t 10.5) + 11.5$
- 4 **a**  $H \doteq 7 \sin \frac{\pi}{6} (t 3.1)$ **b**  $7 \stackrel{H}{\vdash}$



page 792 Review set 13A

5  $T \doteq 7.05 \sin \frac{\pi}{6} (t - 10.5) + 24.75$ 

page 793 Exercise 14E.2

5 b  $\begin{bmatrix} 78669.5\\65589 \end{bmatrix}$  income from day 1 income from day 2

page 803 Exercise 17B.2

**2 b** 
$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -2 \\ 6 \end{bmatrix} + \frac{t}{10} \begin{bmatrix} 20 \\ 15 \end{bmatrix}$$

page 810 Exercise 19L

5 a 
$$\frac{1}{10}$$

page 817 Exercise 23C

$$2 h \frac{1}{x \ln x}$$

page 825 Exercise 29B

1 e 
$$2\sqrt{x-1} - 2\arctan(\sqrt{x-1}) + c$$